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Correlation Between Bridge Vibration And Bridge Deck Cracking: A Qualitative Study

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**CORRELATION BETWEEN BRIDGE VIBRATION AND
BRIDGE DECK CRACKING: A QUALITATIVE STUDY**

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ABSTRACT

In recent years, many New York State bridge engineers have suspected that bridge vibration induced by vehicular traffic significantly influenced deck cracking. Several remedial measures were considered, including modifying the deflection criteria recommended by AASHTO bridge design standards, which would have had a major impact on construction costs. The New York State Department of Transportation initiated a research project to systematically study the possible correlation between bridge deck cracking and bridge vibration. Vibration and cracking severities of most steel girder bridges with concrete decks, built in New York between 1990 and 1997, were obtained through a statewide survey and field inspection. Data were analyzed using statistical methods. Results indicate a strong correlation between bridge vibration and deck cracking. A recommendation to further study this relation, using quantitative data was made. Since this is an observational study, these correlations do not imply that bridge vibration is the primary cause of the bridge deck cracking.

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I. INTRODUCTION

A. BACKGROUND

The New York State Department of Transportation (NYSDOT) continuously studies various factors adversely affecting the structural integrity of its bridges, as part of continuous efforts to improve the quality of New York's transportation infrastructure system. Bridge decks are one such component. Bridge deck cracking has historically been an issue for transportation agencies worldwide due to its role in reducing structural life. Water, laden with de-icing salt, permeates through cracks in the bridge deck and significantly accelerates the degradation of concrete decks. The structure's useful life is reduced and bridge maintenance needs are increased.

Recently, the NYSDOT has improved bridge deck quality by reducing deck permeability and cracking potential through improved concrete properties, deck design, and construction procedures. Some of these changes include pozzuolanic substitutions (fly-ash and micro-silica) for a portion of cement used in bridge deck concrete (1,2), use of isotropically reinforced bridge decks (3), and changing the relative position of longitudinal and transverse reinforcement in the bridge deck (4). These changes positively influenced the deck quality, but did not eliminate the deck cracking (1).

Field engineers consider bridge vibration induced by the vehicular traffic a major factor influencing the bridge deck cracking. This study, therefore, focused on examining the possible relationship between bridge vibration and deck cracking. Parameters defining the vibration are amplitude, frequency, and characteristics of the vehicular traffic. However, recent studies concluded that characteristics of the vehicular traffic do not play a significant role in bridge vibration (5), and therefore it was not considered as a variable in this study.

B. STUDY OBJECTIVE

The objective of this research was to conduct a qualitative study to ascertain if a correlation existed between bridge vibration and bridge deck cracking. If results indicate that bridge vibration does influence deck cracking, then the intent is to determine which bridges are deemed critical for further analysis. This requires defining a frame work for a follow-up quantitative study, which includes field testing of a small number of bridges representing the bridge population in New York State.

The scope of the project is limited to qualitative study of bridges, with concrete decks on steel stringers, built since 1990. Note that this is an observational study, and thus, a correlation between bridge vibration and deck cracking does not imply that bridge vibration is the primary cause of the bridge deck cracking.

C. STUDY APPROACH

A decision to obtain data on the extent of cracking and vibration experienced by each of the bridge decks in New York State was made after consultation with the Structural Engineering Services Unit of the Structures Design and Construction Division. Analysis of the data would reveal if any correlation exists between deck cracking and vibration. New York State has more than 10,000 bridges. An in-depth survey evaluating the decks of all the state's bridges is not feasible. After discussions with bridge engineers, the study was limited to steel girder superstructures built between 1990 and 1997.

A roster of bridges was prepared using the Department's database and sent to field engineers for investigation. Bridge inspectors were asked to physically inspect each of their assigned bridge decks, and report on the existence of deck cracking (type and severity) and bridge vibration (severity). Guidelines were provided for rating deck cracking and vibration. These guidelines are described in the next section.

For each of the selected bridges, various other parameters were determined. Some parameters were obtained from the New York State's bridge inventory and inspection system (BIIS), and others were obtained through a survey questionnaire. The parameters included average annual daily traffic (AADT), number of spans, length of each span, and type of bearing at the beginning and end of each span. Other data collected from engineer-in-charge records and visual inspection of the bridges included environmental conditions during the deck pour, curing methods used, whether or not staged construction was used, and whether the bridge was poured in sections or continuously.

Once the results were compiled, statistical methods were used to examine if a relationship between bridge vibration and deck cracking exists. The next course of action is dependant on the results of this analysis. If there is a statistically significant relationship reported between the bridge vibration and the deck cracking, further experimental studies are warranted to determine which bridge features associated with bridge vibration are playing a major role in deck cracking. If no statistical relationship is found, then an investigation into other possible causes of deck cracking is needed.

II. STATEWIDE SURVEY

A survey questionnaire was prepared and sent to field engineers. The information that was collected by visual inspection included the severity of deck cracking, type of cracking, and severity of bridge vibration. Field engineers were requested to make a field visit to visually inspect the bridge for reporting the deck cracking and bridge vibration severities for each of the spans.

Visual inspections are very subjective in nature. In order to decrease the subjectivity involved with this type of inspection and data collection process, an arbitrary severity rating system was prepared and provided to each bridge inspector along with the questionnaire. Severity ratings were based on a scale from 0 to 5 (5 being the most severe). Detailed definitions of the rating system used are described below.

A. DECK CRACKING SEVERITY RATING

Three categories of cracking were considered in this study. They are longitudinal cracking, transverse cracking and an overall rating to evaluate the extent of cracking on the entire span. A scale of 0 to 5 was used to rate the deck cracking severity as follows:

0. No cracking
1. Low severity
2. Used to shade between ratings of 1 and 3
3. Moderate severity
4. Used to shade between ratings of 3 and 5
5. High severity

Longitudinal cracks: These are the cracks predominantly parallel to the bridge deck centerline. The length of the cracks was measured in meters and width was measured in millimeters. The longitudinal crack ratings are explained below and shown in Figure 1.

Low severity (1) -- Bridge deck exhibits partial length longitudinal cracking. Cracks do not run for more than one-third of the length of the span. Cracks are less than 1 mm wide.

Moderate severity (3) -- Bridge deck exhibits some full length longitudinal cracks. Most cracks are partial length. Most cracks are less than 1 mm wide. Longitudinal cracks occur every 3-4 meters along the cross section of the bridge.

High severity (5) -- Bridge deck exhibits mostly full length longitudinal cracks. Most cracks are wider than 1mm. Cracks occur every 2-3 meters along the cross section of the bridge.

Transverse cracks: These cracks are predominantly perpendicular to the bridge deck centerline. "Y" cracks are counted as a single crack. The length and width of the crack were measured in meters and millimeters, respectively. The transverse crack ratings are explained below and shown in Figure 2.

Low severity (1) -- Bridge deck exhibits mostly partial width transverse cracks. The cracks are less than 1 mm wide.

Moderate severity (3) -- Bridge deck exhibits partial and full width transverse cracks. Cracks are mostly less than 1 mm wide. Transverse cracks occur every 5 meters.

High severity (5) -- Bridge deck exhibits full width transverse cracks with widths greater than 1mm. Some partial width cracking is also evident. Transverse cracks occur every 2-3 meters. Significant "Y" cracking at edges.

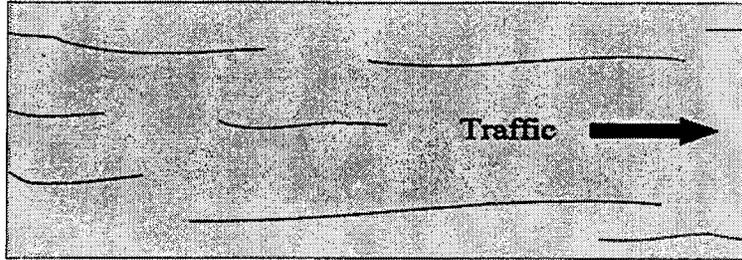
Overall cracking severity: The same rating system was used to rate the entire deck. The rating was increased by 1 if there was significant spalling, map cracking, or durability cracking. Severity ratings were characterized by a 4 or 5 if significant transverse and longitudinal cracking existed. A description of the localized cracking was documented along with appropriate severity levels when localized cracking was present.

B. BRIDGE VIBRATION SEVERITY RATING

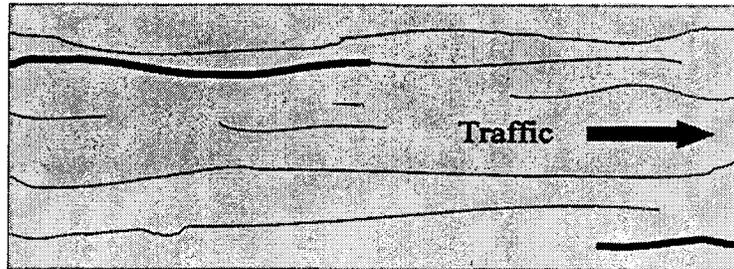
Deck vibration was also rated on a scale of 1 to 5. Low vibrations induced by traffic loads were rated as 1 (low severity), moderate vibrations were rated as 3 (moderate severity), and very noticeable vibrations were rated as 5 (high severity). A rating of 2 was used to shade between 1 and 3, and 4 was used to shade between 3 and 5.

It is not easily possible or practical to quantitatively evaluate/measure bridge vibration (both amplitude and frequency) through visual inspection or with simple instrumentation by field personnel. Hence, it should be noted that these ratings are more subjective and make the results of the study qualitative.

Low Severity (1): Longitudinal Cracking



Moderate Severity (3): Longitudinal Cracking



High Severity (5): Longitudinal Cracking

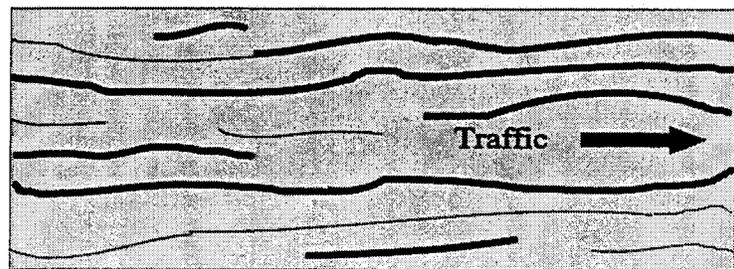
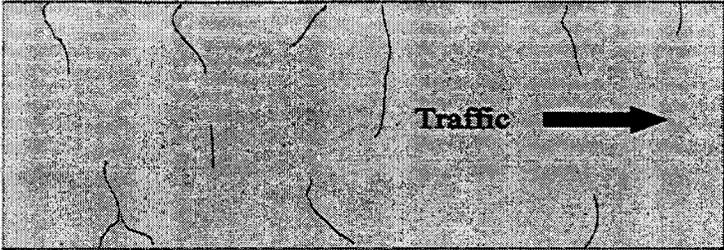
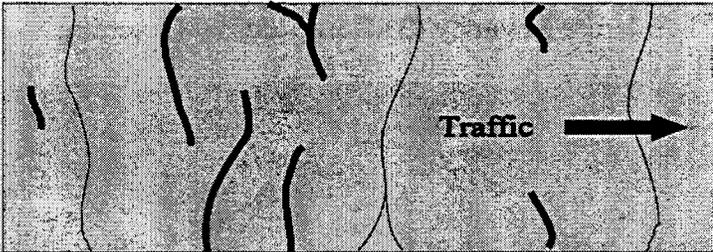


Figure 1. Longitudinal cracking severity guide.

Low Severity (1): Transverse Cracking



Moderate Severity (3): Transverse Cracking



High Severity (5): Transverse Cracking

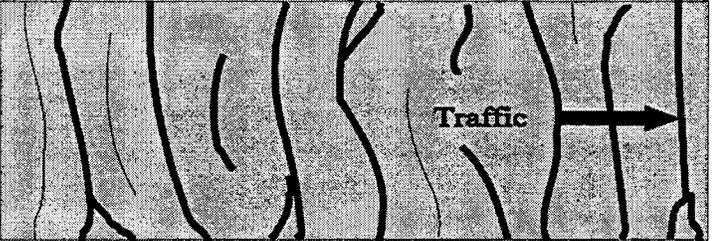


Figure 2. Transverse cracking severity guide.

III. SURVEY RESULTS

A total of 384 bridge spans were inspected by field engineers. Their responses are summarized in Appendix A. This section provides salient details of the raw data pertaining to the inspected bridge population. Results from the statistical analysis will be discussed in the next section.

Figure 3 shows the number of bridge spans in the population sorted by the year constructed; and thus is indicative of the years the bridge is in-service. Of the 384 bridge spans (233 bridges) inspected, 242 exhibited some form of cracking. Figure 4 shows the number of bridges along with their deck cracking severity rating. Two hundred-twenty-seven decks cracked transversely, 44 cracked longitudinally, and 29 bridge decks exhibited both forms of cracking. Environmental conditions during the deck pour, curing procedures used, and construction information were not provided for all the bridges. For this reasons, these data were not used in the further analysis. However, these details will be helpful to compare this information with the severity ratings in a secondary analysis. Figure 5 shows the number of bridge spans in each of the vibration severity ratings.

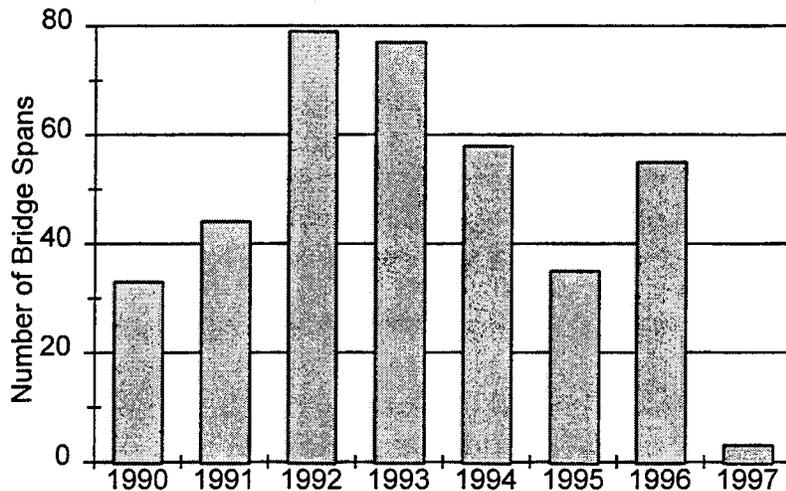


Figure 3. Inspected bridge spans sorted by year constructed.

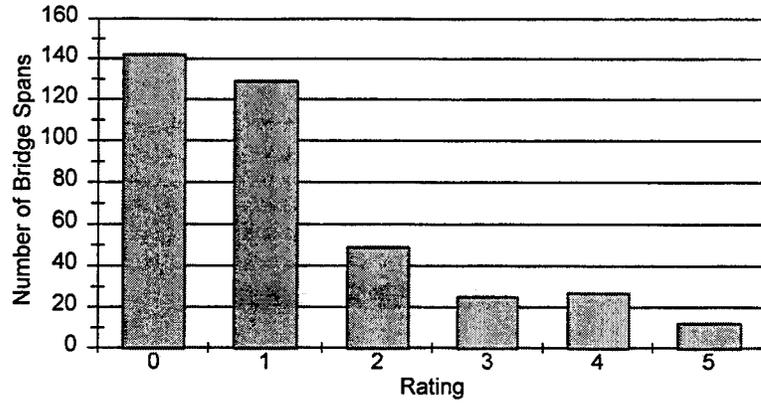


Figure 4. Inspected bridge spans sorted by crack rating.

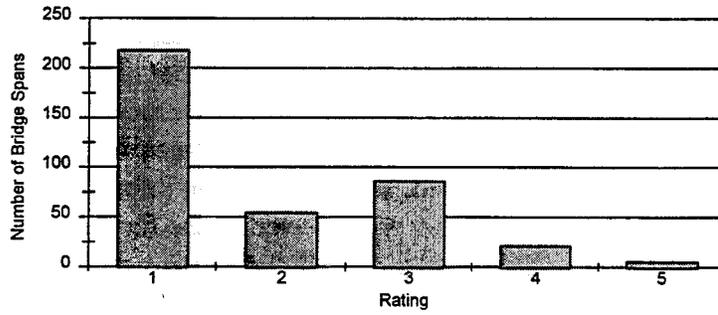


Figure 5. Inspected bridge spans sorted by vibration rating.

IV. DATA ANALYSIS

Statistical methods were used to analyze the responses from the survey. One inspection survey was not included in the analysis due to incomplete data. Thus, only data from 383 bridges were analyzed and the results are presented in this section.

First, One-way Analysis of Variance (ANOVA) was used to study the correlation of each of the following parameters on deck cracking severity (δ).

1. Vibration severity
2. Traffic volume
3. Span length
4. Beginning bearing type
5. End-bearing type

Statgraphics software (7) was used to perform the required calculations and plot graphs. The effects of the individual parameters on deck cracking were first determined. Then multi-factor ANOVA analyses were used to examine the effects of two or more factors on one variable (i.e. deck cracking). The interaction effects of bridge vibration, span length, and traffic volume on bridge deck cracking were examined using Multi-factor ANOVA analyses.

A. EFFECT OF VIBRATION SEVERITY

A careful examination of the vibration data shown in Figure 5 indicates very few bridges with vibration ratings of 4 and 5. In order to make the statistical analysis valid, the vibration ratings (CVIB) were reduced into three groups, by combining ratings of 2 and 3 into one group; and ratings of 4 and 5 into another group as shown in Fig. 6.

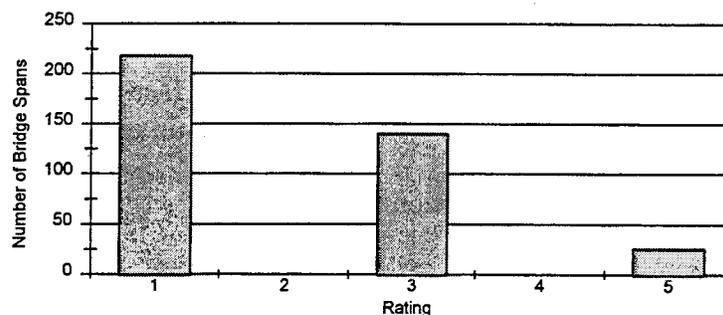


Figure 6. Inspected bridge spans sorted by modified vibration rating.

As described above, a one-way Analysis of Variance was performed to determine the correlation between vibration severity (CVIB) and observed deck cracking severity (SEV). The test results concluded that the vibration severity influences the cracking severity significantly. Detailed analysis is shown in Appendix B.

B. EFFECT OF TRAFFIC VOLUME

The traffic volume data used in the analysis, i.e. Average Annual Daily Traffic (AADT), was classified into three groups:

1. Low volume: $AADT \leq 1000$
2. Medium volume: $1000 < AADT \leq 5000$, and
3. High volume: $AADT > 5000$

Analysis (see Appendix B) indicated that AADT does influence the cracking severity and very low volume bridges exhibit less cracking. This confirms what is expected from practice. At the same time, there is no statistically significant differences between cracking of medium and high volume bridges, indicating that they can be combined for further analysis. Thus, for a multi-factor ANOVA, only two groups will be used, low volume ($AADT \leq 1000$) and high volume ($AADT > 1000$).

C. EFFECT OF SPAN LENGTH

The bridge spans were classified based on their length into following three groups for analysis:

1. Long span bridges: Span Length > 60 m
2. Medium span bridges: $30 \text{ m} < \text{Span Length} \leq 60$ m
3. Small span bridges: Span Length ≤ 30 m

Results (see Appendix B) indicated that span length does influence the cracking severity, with longer spans exhibiting more cracking. The results also showed that there is no statistically significant differences between cracking of bridges with spans less than 30-m long, and spans between 30 m to 60 m long, indicating that they can be combined. Thus, for a multi-factor ANOVA, only two groups of span lengths will be used, spans 60 m or shorter, and spans longer than 60 m.

D. EFFECT OF BEARINGS

Influence of bearings on deck cracking severity was examined (see Appendix B). Since there are many different types of bearings, they were classified into 6 main groups, as follows:

1. Elastomeric Bearing (Free/Expansion)
2. Elastomeric Bearing (Fixed)
3. Pot Bearing (Fixed)
4. Pot Bearing (Free/Expansion)
5. None
6. Others (include discs, rockers, multi-rotational, etc.)

Analysis similar to that described previously was conducted for beginning and end bearing influence on deck cracking. Results indicated that there is no statistically significant difference between the cracking severity and type of bearing. Thus, type of bearing is not considered in further analysis.

E. INTERACTION EFFECTS

Multi-factor ANOVA is useful in examining the effects of two or more factors on one variable. Thus, multi-factor ANOVA is used here to examine the effects of bridge vibration, span length, and traffic volume (AADT) on bridge deck cracking. As illustrated in the previous section, bridge vibration is divided into 3 ranges - low, medium, and noticeable or severe. The traffic volume was divided into 2 categories - low with $AADT \leq 1000$, and high with $AADT > 1000$. Similarly, span lengths have been divided into two categories - short spans with lengths ≤ 60 m, and large spans which are longer than 60 m.

This analysis (see Appendix B) determines the factors having a statistically significant effect on deck cracking, and also tests for significant interactions among the factors considered. The results indicated that vibration severity and span length have a statistically significant effect on bridge deck cracking in the 95% confidence level. Overall, bridges with noticeable vibration combined with long span lengths exhibit significant bridge deck cracking.

V. CONCLUSIONS

Correlation between bridge vibration and bridge deck cracking was studied through field inspection of 384 steel bridge spans with concrete decks. The influence of span length, bearing type, and traffic volume on the deck cracking were investigated along with bridge vibration. The scope of the project is limited to the qualitative study of bridges with concrete decks on steel stringers, constructed between 1990 and 1997. The results indicate the following:

1. Vibration severity is the most significant parameter influencing bridge deck cracking. Higher severity equates to higher deck cracking. Decks with noticeable vibration cracked most severely.
2. Longer spans exhibit more deck cracking than shorter spans.
3. Traffic volume is the least significant factor, of the three considered, in influencing the bridge deck cracking. But, high traffic volume generated more cracking than low traffic volume.
4. Bridge bearings do not influence the deck cracking severity.
5. Bridges with noticeable vibration combined with longer span lengths exhibited significant bridge deck cracking.

Due to the subjective nature of the vibration severity indicator used, further experimental studies are warranted to determine the quantitative effect of bridge vibration on bridge deck cracking, and the role of other structural features on deck cracking associated with bridge vibration.

VI. RECOMMENDATIONS

The results indicate that bridge vibration influences deck cracking. The bridges with noticeable vibration and longer spans may induce more bridge deck cracking. Since vibration response severities were qualitative indices, quantitative data should be obtained for a sample of bridges. Since resources are limited, vibration data collection from the following bridges is recommended (see Table 1). This list was generated using stratified random sampling principles and represent the bridge population under each modified vibration severity rating and span length categories (8).

Table 1. Randomly selected bridges to be field tested.

| Bridge ID (BIN) | Cracking Severity (Rating) | Vibration Severity (Rating) | Traffic Volume (AADT) | Span Length (m) |
|-----------------|----------------------------|-----------------------------|-----------------------|-----------------|
| 4005580 | 5 | 5 | 13750 | 77 |
| 4005580 | 5 | 5 | 13750 | 63 |
| 1093109 | 2 | 3 | 4650 | 34 |
| 1002760 | 2 | 3 | 2857 | 39 |
| 4020060 | 4 | 3 | 9541 | 67 |
| 1010550 | 0 | 1 | 10785 | 23 |
| 1074732 | 1 | 1 | 1000 | 48 |
| 1035670 | 1 | 1 | 2212 | 39 |
| 2260640 | 1 | 3 | 5700 | 69 |
| 1074812 | 0 | 1 | 13500 | 25 |
| 1048090 | 4 | 1 | 1944 | 65 |
| 3331460 | 1 | 1 | 4758 | 58 |
| 2220210 | 1 | 3 | 4452 | 36 |
| 3368130 | 1 | 2 | 5600 | 53 |
| 1041160 | 2 | 4 | 3980 | 35 |
| 1091321 | 3 | 4 | 6925 | 28 |
| 1077100 | 3 | 1 | 12417 | 66 |
| 1026390 | 0 | 1 | 1511 | 34 |
| 1019900 | 0 | 1 | 2093 | 26 |
| 1077160 | 0 | 1 | 11972 | 26 |

Measurement of displacements and accelerations induced by ambient traffic, and the first three modal frequencies of the selected bridges is recommended. These data can be used to get quantitative information on the influence of bridge vibration on deck cracking. They can also be compared with known vehicular vibration characteristics to eliminate resonance issues affecting bridge deck cracking.

ACKNOWLEDGMENTS

The author gratefully acknowledges the bridge inspectors for inspecting each of the bridges selected for this study and collecting relevant data. Frank Owens, formerly with the Department, contributed significantly in the initial stages of the study, preparation of the survey, and data collection. Duane Carpenter of the Structures Design and Construction Division assisted in extracting the bridge information from the bridge inventory database. Joseph C. Savoie of the Structures Design and Construction Division provided necessary input at all stages of this study. Dr. Deniz Sandhu of the Transportation Research and Development Bureau provided advice in conducting the statistical analysis, and Dr. Jorge Haddock of the Rensselaer Polytechnic Institute reviewed the report.

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APPENDIX A
SURVEY RESULTS

SURVEY RESULTS

| BIN (Note 1) | AADT | PAN LENGTH (ft) | BEGINNING BEARING | END BEARING | CRACKED | LONG | TRANS | CRACKING SEVERITY | VIBRATION SEVERITY |
|-----------------|-------|--------------------|----------------------|------------------|---------|------|-------|----------------------|-----------------------|
| 1007540 | 7376 | 93 | EXP Elastomeric | FIX Elastomeric | N | N | N | 0 | 3 |
| 1017990 | 3574 | 160 | EXP Elastomeric | FIX Elastomeric | Y | N | Y | 1 | 1 |
| 1020480 | 885 | 192 | EXP Pot Bearing | FIX Pot Bearing | Y | N | Y | 1 | 3 |
| 1020630 | 4417 | 67 | FIX Elastomeric | EXP Elastomeric | N | N | N | 0 | 2 |
| 1022450 | 9100 | 140 | None | None | Y | Y | Y | 1 | 3 |
| 1022550 | 2030 | 66 | FIX Elastomeric | EXP Elastomeric | Y | N | Y | 1 | 1 |
| 1024710 | 6913 | 200 | FIX Disc Bearing | EXP Disc Bearing | Y | Y | Y | 4 | 2 |
| 1025310 | 11785 | 185 | EXP Pot Bearing | EXP Pot Bearing | N | N | N | 0 | 3 |
| 1025310 | 11785 | 225 | None | FIX Pot Bearing | N | N | N | 0 | 3 |
| 1025310 | 11785 | 265 | None | EXP Pot Bearing | N | N | N | 0 | 3 |
| 1025310 | 11785 | 225 | None | EXP Pot Bearing | N | N | N | 0 | 3 |
| 1025310 | 11785 | 185 | None | EXP Pot Bearing | N | N | N | 0 | 3 |
| 1026300 | 12662 | 50 | EXP Elastomeric | FIX Elastomeric | N | N | N | 0 | 3 |
| 1026300 | 12662 | 70 | None | EXP Elastomeric | N | N | N | 0 | 3 |
| 1026300 | 12662 | 50 | None | EXP Elastomeric | N | N | N | 0 | 3 |
| 1026320 | 13358 | 120 | FIX Pot Bearing | EXP Pot Bearing | Y | Y | Y | 1 | 3 |
| 1033281 | 10041 | 120 | EXP Elastomeric | FIX Elastomeric | Y | Y | Y | 1 | 4 |
| 1033282 | 10041 | 120 | EXP Elastomeric | FIX Elastomeric | Y | Y | Y | 1 | 4 |
| 1038690 | 2857 | 174 | EXP Pot Bearing | FIX Pot Bearing | Y | N | Y | 1 | 2 |
| 1054150 | 9600 | 184 | EXP Pot Bearing | EXP Pot Bearing | Y | N | Y | 3 | 3 |
| 1093109 | 4650 | 125 | EXP Elastomeric | FIX Elastomeric | Y | N | Y | 2 | 3 |
| 1093109 | 4650 | 111 | None | EXP Elastomeric | Y | N | Y | 2 | 3 |
| 2200460 | 12300 | 72 | EXP Elastomeric | FIX Elastomeric | Y | N | Y | 1 | 2 |
| 3200600 | 50 | 121 | FIX Elastomeric | EXP Elastomeric | N | N | N | 0 | 2 |
| 3300920 | 106 | 89 | FIX Elastomeric | EXP Elastomeric | N | N | N | 0 | 1 |
| 3301740 | 250 | 135 | FIX Elastomeric | EXP Elastomeric | N | N | N | 0 | 2 |
| 3303080 | 971 | 90 | EXP Pot Bearing | FIX Pot Bearing | Y | N | Y | 1 | 1 |
| 3303080 | 971 | 165 | FIX Pot Bearing | EXP Pot Bearing | Y | N | Y | 1 | 1 |
| 3304000 | 640 | 185 | FIX Elastomeric | EXP Elastomeric | N | N | N | 0 | 1 |
| 3305510 | 4550 | 148 | EXP Elastomeric | EXP Elastomeric | Y | Y | Y | 3 | 2 |
| 3305510 | 4550 | 185 | None | FIX Elastomeric | Y | Y | Y | 3 | 2 |
| 3305510 | 4550 | 185 | None | EXP Elastomeric | Y | Y | Y | 3 | 2 |
| 3305510 | 4550 | 148 | None | EXP Elastomeric | Y | Y | Y | 3 | 2 |
| 3368290 | 4550 | 144 | EXP Pot Bearing | FIX Pot Bearing | Y | N | Y | 2 | 1 |
| 3368290 | 4550 | 144 | FIX Pot Bearing | EXP Pot Bearing | Y | N | Y | 2 | 1 |
| 3368290 | 4550 | 144 | EXP Pot Bearing | FIX Pot Bearing | Y | N | Y | 2 | 1 |
| 3368290 | 4550 | 144 | FIX Pot Bearing | EXP Pot Bearing | Y | N | Y | 2 | 1 |
| 3368290 | 4550 | 139 | EXP Pot Bearing | FIX Pot Bearing | Y | N | Y | 2 | 1 |
| 3368290 | 4550 | 180 | FIX Pot Bearing | EXP Pot Bearing | Y | N | Y | 2 | 1 |
| 3368290 | 4550 | 139 | EXP Pot Bearing | EXP Pot Bearing | Y | N | Y | 2 | 1 |
| 4005580 | 13750 | 207 | EXP Pot Bearing | EXP Pot Bearing | Y | N | Y | 5 | 5 |
| 4005580 | 13750 | 253 | None | EXP Pot Bearing | Y | N | Y | 5 | 5 |
| 4005580 | 13750 | 300 | None | FIX Pot Bearing | Y | N | Y | 5 | 5 |
| 4005580 | 13750 | 253 | None | EXP Pot Bearing | Y | N | Y | 5 | 5 |
| 4005580 | 13750 | 207 | None | EXP Pot Bearing | Y | N | Y | 5 | 5 |

| | | | | | | | | | |
|---------|-------|-----|-------------------|------------------|---|---|---|-----|-----|
| 1002760 | 2857 | 127 | FIX Pot Bearing | EXP Pot Bearing | Y | N | Y | 2 | 2.5 |
| 1002760 | 2857 | 139 | None | EXP Pot Bearing | Y | N | Y | 2 | 2.5 |
| 1002760 | 2857 | 144 | None | EXP Pot Bearing | Y | N | Y | 2 | 2.5 |
| 1010550 | 10785 | 75 | EXP Elastomeric | FIX Elastomeric | N | N | N | 0 | 1 |
| 1010630 | 9341 | 96 | FIX Elastomeric | EXP Elastomeric | N | N | N | 0 | 1 |
| 1018861 | 1374 | 150 | EXP Pot Bearing | FIX Pot Bearing | Y | N | Y | 2 | 4 |
| 1018861 | 1374 | 150 | None | EXP Pot Bearing | Y | N | Y | 2 | 4 |
| 1018862 | 1374 | 150 | EXP Pot Bearing | FIX Pot Bearing | Y | N | Y | 2 | 4 |
| 1018862 | 1374 | 150 | None | EXP Pot Bearing | Y | N | Y | 2 | 4 |
| 1020320 | 2010 | 105 | EXP Elastomeric | FIX Elastomeric | Y | N | Y | 2 | 2 |
| 1020320 | 2010 | 105 | None | EXP Elastomeric | Y | N | Y | 2 | 2 |
| 1029360 | 4500 | 59 | None | None | N | N | N | 0 | 1 |
| 1038820 | 1193 | 230 | EXP Pot Bearing | FIX Pot Bearing | Y | N | Y | 1 | 3 |
| 1038820 | 1193 | 230 | None | EXP Pot Bearing | Y | N | Y | 1 | 3 |
| 1052070 | 20144 | 66 | FIX Elastomeric | EXP Elastomeric | N | N | N | 0 | 1 |
| 3307190 | 507 | 42 | FIX Elastomeric | EXP Elastomeric | Y | N | Y | 1 | 1 |
| 3307190 | 507 | 42 | None | EXP Elastomeric | N | N | N | 0 | 1 |
| 4018871 | 11000 | 134 | EXP Pot Bearing | EXP Pot Bearing | N | N | N | 0 | 3 |
| 4018871 | 11000 | 167 | None | EXP Pot Bearing | N | N | N | 0 | 3 |
| 4018871 | 11000 | 146 | None | FIX Pot Bearing | N | N | N | 0 | 3 |
| 4018871 | 11000 | 120 | None | EXP Pot Bearing | N | N | N | 0 | 3 |
| 4018872 | 1374 | 134 | EXP Pot Bearing | EXP Pot Bearing | N | N | N | 0 | 3 |
| 4018872 | 1374 | 167 | EXP Steel Sliding | EXP Pot Bearing | N | N | N | 0 | 3 |
| 4018872 | 1374 | 146 | None | FIX Pot Bearing | N | N | N | 0 | 3 |
| 4018872 | 1374 | 139 | None | EXP Pot Bearing | N | N | N | 0 | 3 |
| 4020060 | 9541 | 220 | EXP Pot Bearing | FIX Pot Bearing | Y | N | Y | 3.5 | 3 |
| 4020060 | 9541 | 220 | None | EXP Pot Bearing | Y | N | Y | 1 | 3 |
| 4020060 | 9541 | 150 | None | EXP Pot Bearing | Y | N | Y | 3 | 3 |
| 1016490 | 3503 | 160 | EXP Disc Bearing | EXP Disc Bearing | N | N | N | 0 | 1 |
| 1016490 | 3503 | 180 | None | FIXED Multi-Rota | N | N | N | 0 | 1 |
| 1016490 | 3503 | 180 | None | EXP Disc Bearing | N | N | N | 0 | 1 |
| 1016490 | 3503 | 180 | None | EXP Disc Bearing | Y | N | Y | 1 | 1 |
| 1016490 | 3503 | 160 | None | EXP Disc Bearing | N | N | N | 0 | 1 |
| 1021720 | 13991 | 132 | EXP Pot Bearing | FIX Pot Bearing | N | N | N | 0 | 1 |
| 1022111 | 23621 | 159 | EXP Disc Bearing | FIXED Multi-Rota | N | N | N | 0 | 1 |
| 1022112 | 23621 | 159 | EXP Disc Bearing | FIXED Multi-Rota | N | N | N | 0 | 1 |
| 1023010 | 4805 | 120 | EXP Elastomeric | FIX Elastomeric | N | N | N | 0 | 1 |
| 1023650 | 4264 | 127 | EXP Elastomeric | FIX Elastomeric | Y | Y | N | 1 | 1 |
| 1025842 | 49234 | 55 | EXP Elastomeric | EXP Elastomeric | Y | N | Y | 1 | 1 |
| 1025842 | 49234 | 62 | None | FIX Elastomeric | Y | N | Y | 1 | 1 |
| 1025842 | 49234 | 45 | None | EXP Elastomeric | N | N | N | 0 | 1 |
| 1025842 | 49234 | 45 | None | EXP Elastomeric | N | N | N | 0 | 1 |
| 1025851 | 49234 | 72 | EXP Elastomeric | EXP Elastomeric | Y | Y | N | 1 | 1 |
| 1025851 | 49234 | 93 | None | FIX Elastomeric | Y | Y | N | 1 | 1 |
| 1025851 | 49234 | 54 | None | EXP Elastomeric | Y | Y | N | 1 | 1 |
| 1025852 | 49234 | 77 | EXP Elastomeric | EXP Elastomeric | Y | Y | N | 1 | 1 |
| 1025852 | 49234 | 98 | None | FIX Elastomeric | Y | Y | N | 1 | 1 |
| 1025852 | 49234 | 57 | None | EXP Elastomeric | Y | Y | N | 1 | 1 |
| 1034220 | 3482 | 150 | Other FIXED | Other FIXED | Y | N | Y | 1 | 1 |
| 1035670 | 2212 | 129 | EXP Elastomeric | FIX Elastomeric | Y | N | Y | 1 | 1 |
| 1035730 | 5472 | 128 | EXP Elastomeric | FIX Elastomeric | Y | N | Y | 4 | 1 |
| 1035730 | 5472 | 128 | None | EXP Elastomeric | Y | N | Y | 4 | 1 |
| 1040291 | 4106 | 106 | FIX Elastomeric | EXP Elastomeric | Y | N | Y | 1 | 3 |
| 1040292 | 4106 | 100 | FIX Elastomeric | EXP Elastomeric | Y | N | Y | 1 | 3 |

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|---------|--------|-----|------------------|------------------|---|---|---|---|---|
| 1043390 | 2561 | 69 | EXP Disc Bearing | FIXED Multi-Rota | Y | N | Y | 1 | 1 |
| 1043390 | 2561 | 130 | None | EXP Disc Bearing | Y | N | Y | 1 | 1 |
| 1043390 | 2561 | 69 | None | EXP Disc Bearing | Y | N | Y | 1 | 1 |
| 1043450 | 14026 | 100 | EXP Disc Bearing | FIXED Multi-Rota | Y | N | Y | 1 | 1 |
| 1043450 | 14026 | 100 | None | EXP Disc Bearing | Y | N | Y | 1 | 1 |
| 1048680 | 14879 | 99 | EXP Pot Bearing | FIX Pot Bearing | Y | N | Y | 1 | 1 |
| 1048680 | 14879 | 99 | None | EXP Pot Bearing | Y | N | Y | 1 | 1 |
| 1048900 | 0 | 150 | EXP Elastomeric | FIX Elastomeric | N | N | N | 0 | 1 |
| 1048929 | 14028 | 137 | EXP Elastomeric | FIX Elastomeric | Y | N | Y | 1 | 1 |
| 1048929 | 14028 | 104 | None | EXP Elastomeric | Y | N | Y | 1 | 1 |
| 1060620 | 7264 | 102 | EXP Elastomeric | Other FIXED | Y | Y | N | 1 | 1 |
| 1060620 | 7264 | 102 | None | Other FIXED | Y | Y | N | 1 | 1 |
| 1060620 | 7264 | 102 | None | EXP Elastomeric | Y | Y | Y | 1 | 1 |
| 1074690 | 8377 | 105 | EXP Elastomeric | FIX Elastomeric | Y | N | Y | 1 | 1 |
| 1074690 | 8377 | 105 | None | EXP Elastomeric | Y | N | Y | 1 | 1 |
| 1074701 | 600500 | 111 | FIX Elastomeric | EXP Elastomeric | Y | Y | Y | 1 | 1 |
| 1074702 | 500 | 111 | FIX Elastomeric | EXP Elastomeric | Y | Y | Y | 1 | 1 |
| 1074710 | 1000 | 105 | EXP Elastomeric | FIX Elastomeric | Y | N | Y | 1 | 1 |
| 1074710 | 1000 | 105 | None | EXP Elastomeric | Y | N | Y | 1 | 1 |
| 1074731 | 1000 | 156 | FIX Pot Bearing | EXP Pot Bearing | Y | N | Y | 1 | 1 |
| 1074732 | 1000 | 156 | FIX Pot Bearing | EXP Pot Bearing | Y | N | Y | 1 | 1 |
| 2034240 | 10537 | 108 | EXP Elastomeric | FIX Elastomeric | N | N | N | 0 | 3 |
| 2034240 | 10537 | 72 | None | EXP Elastomeric | N | N | N | 0 | 3 |
| 2257760 | 1268 | 110 | FIX Pot Bearing | EXP Pot Bearing | N | N | N | 0 | 1 |
| 3317890 | 1621 | 121 | EXP Elastomeric | FIX Elastomeric | N | N | N | 0 | 1 |
| 3319010 | 1410 | 96 | FIX Elastomeric | EXP Elastomeric | Y | N | Y | 1 | 1 |
| 4011030 | 8643 | 180 | EXP Pot Bearing | FIX Pot Bearing | N | N | N | 0 | 1 |
| 4443330 | 12514 | 170 | EXP Pot Bearing | FIX Pot Bearing | Y | Y | N | 1 | 1 |
| 4443350 | 9291 | 160 | EXP Elastomeric | FIX Elastomeric | Y | N | Y | 1 | 1 |
| 1001210 | 2948 | 55 | EXP Elastomeric | FIX Elastomeric | Y | N | Y | 1 | 1 |
| 1011660 | 6274 | 82 | EXP Pot Bearing | EXP Pot Bearing | N | N | N | 0 | 1 |
| 1011660 | 6274 | 140 | None | FIX Pot Bearing | N | N | N | 0 | 1 |
| 1011660 | 6274 | 82 | None | EXP Pot Bearing | N | N | N | 0 | 1 |
| 1012350 | 15379 | 86 | None | None | N | N | N | 0 | 1 |
| 1022920 | 16237 | 147 | EXP Pot Bearing | FIX Pot Bearing | Y | N | Y | 1 | 3 |
| 1024550 | 3522 | 90 | EXP Elastomeric | FIX Elastomeric | N | N | Y | 0 | 1 |
| 1027830 | 7019 | 146 | FIX Pot Bearing | EXP Pot Bearing | Y | Y | Y | 1 | 1 |
| 1027870 | 7450 | 163 | EXP Elastomeric | FIX Elastomeric | Y | Y | Y | 3 | 3 |
| 1028200 | 5699 | 150 | EXP Pot Bearing | EXP Pot Bearing | Y | N | Y | 1 | 1 |
| 1028200 | 5699 | 190 | None | FIX Pot Bearing | Y | N | Y | 4 | 3 |
| 1028200 | 5699 | 190 | None | EXP Pot Bearing | Y | N | Y | 3 | 2 |
| 1028200 | 5699 | 150 | None | EXP Pot Bearing | Y | N | Y | 3 | 2 |
| 1028200 | 5699 | 133 | EXP Pot Bearing | FIX Pot Bearing | Y | N | Y | 1 | 1 |
| 1028200 | 5699 | 165 | None | EXP Pot Bearing | Y | N | Y | 3 | 2 |
| 1028200 | 5699 | 133 | None | EXP Pot Bearing | Y | N | Y | 4 | 2 |
| 1030180 | 4208 | 161 | None | None | N | N | N | 0 | 1 |
| 1041520 | 6300 | 89 | FIX Elastomeric | EXP Elastomeric | N | N | N | 0 | 1 |
| 1042560 | 12508 | 69 | None | None | Y | Y | Y | 1 | 1 |
| 1044230 | 30300 | 54 | EXP Elastomeric | FIX Elastomeric | Y | N | Y | 1 | 1 |
| 1044230 | 30300 | 80 | None | EXP Elastomeric | Y | N | Y | 1 | 1 |
| 1044230 | 30300 | 54 | None | EXP Elastomeric | Y | N | Y | 1 | 1 |
| 1071471 | 3538 | 105 | EXP Elastomeric | FIX Elastomeric | Y | Y | Y | 3 | 3 |
| 1071501 | 3538 | 138 | EXP Elastomeric | FIX Elastomeric | Y | Y | N | 1 | 1 |
| 1074561 | 8769 | 140 | FIX Elastomeric | EXP Elastomeric | N | N | N | 0 | 1 |

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|---------|-------|-----|-----------------|-----------------|---|---|---|---|-----|
| 1074562 | 8769 | 140 | FIX Elastomeric | EXP Elastomeric | N | N | N | 0 | 1 |
| 2260580 | 1355 | 81 | FIX Elastomeric | EXP Elastomeric | Y | N | Y | 1 | 1 |
| 2260640 | 5700 | 219 | EXP Pot Bearing | FIX Pot Bearing | Y | N | Y | 1 | 3 |
| 2260640 | 5700 | 219 | None | EXP Pot Bearing | Y | N | Y | 1 | 3 |
| 2260640 | 5700 | 191 | EXP Pot Bearing | EXP Pot Bearing | Y | N | Y | 1 | 3 |
| 2260640 | 5700 | 226 | None | FIX Pot Bearing | Y | N | Y | 1 | 3 |
| 2260640 | 5700 | 226 | None | EXP Pot Bearing | Y | N | Y | 1 | 3 |
| 2260640 | 5700 | 191 | None | EXP Pot Bearing | Y | N | Y | 1 | 3 |
| 2263810 | 839 | 76 | EXP Pot Bearing | EXP Pot Bearing | N | N | N | 0 | 1 |
| 2263810 | 839 | 104 | None | FIX Pot Bearing | N | N | N | 0 | 1 |
| 2263810 | 839 | 104 | None | EXP Pot Bearing | N | N | N | 0 | 1 |
| 2263810 | 839 | 76 | None | EXP Pot Bearing | N | N | N | 0 | 1 |
| 3027760 | 5140 | 109 | EXP Pot Bearing | FIX Pot Bearing | Y | N | Y | 1 | 1 |
| 3027760 | 5140 | 109 | None | EXP Pot Bearing | Y | N | Y | 1 | 1 |
| 3324840 | 978 | 195 | EXP Pot Bearing | FIX Pot Bearing | N | N | N | 0 | 1 |
| 3326910 | 1000 | 140 | EXP Elastomeric | FIX Elastomeric | N | N | N | 0 | 1 |
| 3326990 | 8809 | 95 | None | None | Y | Y | Y | 1 | 1 |
| 3327100 | 1000 | 120 | EXP Elastomeric | FIX Elastomeric | Y | N | Y | 1 | 1 |
| 3327920 | 3760 | 115 | EXP Elastomeric | FIX Elastomeric | N | N | N | 0 | 1 |
| 3328390 | 315 | 178 | FIX Pot Bearing | EXP Pot Bearing | N | N | N | 0 | 1 |
| 3368440 | 4100 | 122 | None | None | N | N | N | 0 | 1 |
| 4454030 | 4735 | 73 | None | EXP Pot Bearing | N | N | N | 0 | 1 |
| 4454030 | 4735 | 119 | None | EXP Pot Bearing | Y | N | Y | 4 | 3 |
| 4454030 | 4735 | 73 | None | None | N | N | N | 0 | 1 |
| 4454090 | 1062 | 76 | EXP Elastomeric | EXP Elastomeric | N | N | N | 0 | 1 |
| 4454090 | 1062 | 137 | None | FIX Elastomeric | Y | N | Y | 4 | 3.5 |
| 4454090 | 1062 | 76 | None | EXP Elastomeric | N | N | N | 0 | 1 |
| 4454130 | 5103 | 132 | EXP Elastomeric | FIX Elastomeric | N | N | N | 0 | 1 |
| 4454130 | 5103 | 55 | FIX Elastomeric | EXP Elastomeric | N | N | N | 0 | 1 |
| 6012270 | 5000 | 158 | EXP Elastomeric | FIX Elastomeric | N | N | N | 0 | 1 |
| 1010180 | 8195 | 126 | None | EXP Elastomeric | Y | N | Y | 5 | 3.5 |
| 1010180 | 8195 | 126 | EXP Elastomeric | FIX Elastomeric | Y | N | Y | 5 | 3.5 |
| 1011380 | 1020 | 109 | None | EXP Pot Bearing | N | N | N | 0 | 1 |
| 1011380 | 1020 | 145 | None | EXP Pot Bearing | Y | N | Y | 1 | 1 |
| 1011380 | 1020 | 109 | EXP Pot Bearing | FIX Pot Bearing | N | N | N | 0 | 1 |
| 1012480 | 2528 | 175 | FIX Pot Bearing | EXP Pot Bearing | N | N | N | 0 | 1 |
| 1012520 | 4503 | 80 | None | EXP Pot Bearing | Y | N | Y | 1 | 1 |
| 1012520 | 4503 | 155 | None | EXP Pot Bearing | Y | N | Y | 1 | 1 |
| 1012520 | 4503 | 130 | EXP Pot Bearing | FIX Pot Bearing | Y | N | Y | 1 | 1 |
| 1012550 | 1358 | 130 | FIX Elastomeric | EXP Elastomeric | N | N | N | 0 | 1 |
| 1012660 | 6919 | 82 | None | None | N | N | N | 0 | 1 |
| 1012910 | 3608 | 165 | EXP Elastomeric | FIX Elastomeric | Y | Y | Y | 2 | 1 |
| 1012930 | 11780 | 133 | None | EXP Elastomeric | Y | N | Y | 2 | 2 |
| 1012930 | 11780 | 133 | None | None | Y | N | Y | 2 | 2 |
| 1014940 | 7307 | 124 | None | None | N | N | N | 0 | 2 |
| 1015020 | 5465 | 126 | FIX Pot Bearing | EXP Pot Bearing | Y | Y | N | 1 | 3 |
| 1015050 | 4881 | 153 | None | None | N | N | N | 0 | 1 |
| 1016340 | 7393 | 130 | None | EXP Elastomeric | N | N | N | 0 | 1 |
| 1016340 | 7393 | 130 | EXP Elastomeric | FIX Elastomeric | N | N | N | 0 | 1 |
| 1042860 | 1915 | 127 | EXP Elastomeric | FIX Elastomeric | Y | N | Y | 1 | 1 |
| 1042860 | 1915 | 127 | None | EXP Elastomeric | Y | N | Y | 1 | 1 |
| 1046880 | 1479 | 107 | EXP Elastomeric | FIX Elastomeric | N | N | N | 0 | 1 |
| 1046890 | 1479 | 132 | EXP Elastomeric | FIX Elastomeric | N | N | N | 0 | 1 |
| 1048090 | 1944 | 214 | FIX Pot Bearing | EXP Pot Bearing | Y | Y | Y | 4 | 1 |

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|---------|-------|-----|-----------------|-----------------|---|---|---|-----|---|
| 1074800 | 4000 | 115 | None | EXP Pot Bearing | Y | Y | Y | 1 | 1 |
| 1074800 | 4000 | 175 | None | EXP Pot Bearing | Y | N | Y | 1 | 1 |
| 1074800 | 4000 | 115 | EXP Pot Bearing | FIX Pot Bearing | N | N | N | 0 | 1 |
| 1074811 | 13500 | 83 | FIX Elastomeric | EXP Elastomeric | N | N | N | 0 | 1 |
| 1074812 | 13500 | 83 | FIX Elastomeric | EXP Elastomeric | N | N | N | 0 | 1 |
| 1074821 | 13500 | 104 | FIX Elastomeric | EXP Elastomeric | N | N | N | 0 | 1 |
| 1074822 | 13500 | 104 | FIX Elastomeric | EXP Elastomeric | N | N | N | 0 | 1 |
| 1074830 | 4000 | 128 | FIX Elastomeric | EXP Elastomeric | N | N | N | 0 | 1 |
| 1074840 | 4000 | 128 | FIX Elastomeric | EXP Elastomeric | Y | Y | N | 1 | 1 |
| 1074851 | 13500 | 73 | FIX Elastomeric | EXP Elastomeric | N | N | N | 0 | 1 |
| 1074852 | 13500 | 73 | FIX Elastomeric | EXP Elastomeric | Y | Y | N | 1 | 1 |
| 1074861 | 2873 | 121 | EXP Elastomeric | FIX Elastomeric | Y | N | Y | 1 | 1 |
| 1074862 | 2873 | 115 | EXP Elastomeric | FIX Elastomeric | Y | Y | N | 1 | 1 |
| 1074881 | 2873 | 85 | EXP Elastomeric | FIX Elastomeric | N | N | N | 0 | 1 |
| 1074882 | 2873 | 85 | EXP Elastomeric | FIX Elastomeric | Y | N | Y | 1 | 1 |
| 1074900 | 5300 | 188 | None | EXP Pot Bearing | N | N | N | 0 | 1 |
| 1074900 | 5300 | 191 | EXP Pot Bearing | EXP Pot Bearing | Y | N | Y | 1 | 1 |
| 1074900 | 5300 | 187 | FIX Pot Bearing | EXP Pot Bearing | N | N | N | 0 | 1 |
| 1074900 | 5300 | 191 | None | EXP Pot Bearing | N | N | N | 0 | 1 |
| 1074900 | 5300 | 184 | None | EXP Pot Bearing | N | N | N | 0 | 1 |
| 1074900 | 5300 | 174 | None | FIX Pot Bearing | N | N | N | 0 | 1 |
| 1077150 | 7393 | 127 | EXP Elastomeric | FIX Elastomeric | N | N | N | 0 | 1 |
| 1090980 | 3419 | 131 | None | None | N | N | N | 0 | 1 |
| 2214000 | 1970 | 140 | EXP Elastomeric | FIX Elastomeric | N | N | N | 0 | 1 |
| 2218180 | 1378 | 126 | FIX Elastomeric | EXP Elastomeric | Y | N | Y | 1 | 1 |
| 2218210 | 4186 | 137 | EXP Elastomeric | FIX Elastomeric | N | N | N | 0 | 1 |
| 3331460 | 4758 | 189 | EXP Elastomeric | FIX Elastomeric | Y | N | Y | 1 | 1 |
| 3331460 | 4758 | 134 | None | EXP Elastomeric | Y | N | Y | 1 | 1 |
| 1000780 | 2643 | 176 | FIX Pot Bearing | EXP Pot Bearing | Y | N | Y | 1 | 1 |
| 1000800 | 2643 | 151 | EXP Elastomeric | FIX Elastomeric | Y | N | Y | 2.5 | 2 |
| 1007041 | 4342 | 112 | FIX Pot Bearing | EXP Pot Bearing | Y | N | Y | 3 | 3 |
| 1007042 | 4342 | 112 | FIX Pot Bearing | EXP Pot Bearing | Y | N | Y | 3.5 | 3 |
| 1008550 | 1854 | 131 | None | FIX Pot Bearing | Y | N | Y | 1 | 3 |
| 1008550 | 1854 | 117 | None | EXP Pot Bearing | Y | N | Y | 1 | 3 |
| 1008850 | 1854 | 130 | None | None | Y | N | Y | 1 | 3 |
| 1010170 | 7633 | 105 | None | FIX Elastomeric | Y | N | Y | 1 | 3 |
| 1010170 | 7633 | 118 | None | None | Y | N | Y | 1 | 3 |
| 1017250 | 2213 | 160 | EXP Elastomeric | FIX Elastomeric | Y | N | Y | 4 | 2 |
| 1017250 | 2213 | 160 | None | EXP Elastomeric | Y | N | Y | 4 | 2 |
| 1017299 | 3186 | 122 | EXP Elastomeric | FIX Elastomeric | Y | N | Y | 3 | 2 |
| 1017299 | 3186 | 127 | None | EXP Elastomeric | Y | N | Y | 3 | 2 |
| 1018950 | 2852 | 108 | EXP Elastomeric | FIX Elastomeric | N | N | N | 0 | 2 |
| 1018960 | 4486 | 97 | EXP Elastomeric | FIX Elastomeric | Y | N | Y | 2 | 3 |
| 1018960 | 4486 | 130 | None | EXP Elastomeric | Y | N | Y | 2 | 3 |
| 1018960 | 4486 | 97 | None | EXP Elastomeric | Y | N | Y | 2 | 3 |
| 1021270 | 2109 | 144 | EXP Elastomeric | FIX Elastomeric | Y | N | Y | 3 | 2 |
| 1021270 | 2109 | 171 | None | EXP Elastomeric | Y | N | Y | 3 | 2 |
| 1021280 | 1159 | 127 | None | None | Y | N | Y | 3 | 2 |
| 1023980 | 4089 | 120 | EXP Elastomeric | FIX Elastomeric | Y | N | Y | 1 | 2 |
| 1023980 | 4089 | 120 | None | EXP Elastomeric | Y | N | Y | 1 | 2 |
| 1027250 | 1016 | 120 | EXP Elastomeric | FIX Elastomeric | Y | N | Y | 1 | 3 |
| 1027250 | 1016 | 120 | None | EXP Elastomeric | Y | N | Y | 1 | 3 |
| 1027260 | 2974 | 110 | EXP Elastomeric | FIX Elastomeric | Y | N | Y | 2 | 3 |
| 1027260 | 2974 | 140 | None | EXP Elastomeric | Y | N | Y | 2 | 3 |

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|---------|-------|-----|-----------------|-----------------|---|---|---|---|-----|
| 1027260 | 2974 | 110 | None | EXP Elastomeric | Y | N | Y | 2 | 3 |
| 1027270 | 2938 | 120 | EXP Elastomeric | FIX Elastomeric | Y | N | Y | 2 | 3 |
| 1027270 | 2938 | 120 | None | EXP Elastomeric | Y | N | Y | 2 | 3 |
| 1027560 | 739 | 84 | EXP Elastomeric | FIX Elastomeric | Y | N | Y | 1 | 2 |
| 1062080 | 6103 | 102 | EXP Pot Bearing | EXP Pot Bearing | Y | N | Y | 1 | 3 |
| 1062080 | 6103 | 137 | None | FIX Pot Bearing | Y | N | Y | 1 | 3 |
| 1062080 | 6103 | 102 | None | EXP Pot Bearing | Y | N | Y | 1 | 3 |
| 1074780 | 3526 | 103 | EXP Pot Bearing | EXP Pot Bearing | Y | N | Y | 1 | 3 |
| 1074780 | 3526 | 138 | None | FIX Pot Bearing | Y | N | Y | 1 | 3 |
| 1074780 | 3526 | 103 | None | EXP Pot Bearing | Y | N | Y | 1 | 3 |
| 2219650 | 6514 | 120 | EXP Elastomeric | FIX Elastomeric | Y | N | Y | 3 | 2 |
| 2219650 | 6514 | 120 | None | EXP Elastomeric | Y | N | Y | 3 | 2 |
| 2220210 | 4452 | 119 | EXP Pot Bearing | FIX Pot Bearing | Y | N | Y | 1 | 3 |
| 2220210 | 4452 | 145 | None | FIX Pot Bearing | Y | N | Y | 1 | 3 |
| 2220210 | 4452 | 119 | None | EXP Pot Bearing | Y | N | Y | 1 | 3 |
| 2220220 | 19500 | 237 | EXP Pot Bearing | FIX Pot Bearing | N | N | N | 0 | 2.5 |
| 2220220 | 19500 | 245 | None | EXP Pot Bearing | N | N | N | 0 | 2.5 |
| 3336620 | 456 | 42 | EXP Elastomeric | FIX Elastomeric | N | N | N | 0 | 1 |
| 3338480 | 123 | 148 | FIX Elastomeric | EXP Elastomeric | Y | N | Y | 1 | 3 |
| 3339020 | 5730 | 206 | FIX Pot Bearing | EXP Pot Bearing | Y | N | Y | 1 | 3 |
| 3340620 | 406 | 142 | EXP Elastomeric | FIX Elastomeric | N | N | N | 0 | 2 |
| 1003070 | 2974 | 52 | FIX Elastomeric | EXP Elastomeric | Y | Y | Y | 2 | 2 |
| 1003160 | 8908 | 111 | None | EXP Elastomeric | Y | N | Y | 4 | 3 |
| 1003160 | 8908 | 111 | None | None | Y | N | Y | 4 | 3 |
| 1016671 | 4194 | 129 | EXP Pot Bearing | FIX Pot Bearing | Y | Y | Y | 2 | 2 |
| 1016671 | 4194 | 164 | None | EXP Pot Bearing | Y | Y | Y | 2 | 2 |
| 1016671 | 4194 | 100 | None | EXP Pot Bearing | Y | Y | Y | 2 | 2 |
| 1016672 | 4194 | 125 | EXP Pot Bearing | FIX Pot Bearing | Y | Y | Y | 4 | 3 |
| 1016672 | 4194 | 158 | None | EXP Pot Bearing | Y | Y | Y | 4 | 3 |
| 1016672 | 4194 | 117 | None | EXP Pot Bearing | Y | Y | Y | 4 | 3 |
| 1022349 | 14755 | 56 | EXP Elastomeric | None | Y | N | Y | 5 | 4 |
| 1022349 | 14755 | 69 | EXP Elastomeric | None | Y | N | Y | 5 | 4 |
| 1022349 | 14755 | 34 | EXP Elastomeric | FIX Elastomeric | Y | N | Y | 5 | 4 |
| 1026840 | 7725 | 180 | FIX Elastomeric | EXP Elastomeric | Y | N | Y | 2 | 3 |
| 1034850 | 4495 | 58 | FIX Elastomeric | FIX Elastomeric | N | N | N | 0 | 1 |
| 1037380 | 17440 | 46 | FIX Elastomeric | EXP Elastomeric | Y | N | Y | 2 | 2 |
| 1040801 | 6925 | 95 | EXP Elastomeric | FIX Elastomeric | Y | N | Y | 4 | 4 |
| 1040801 | 6925 | 95 | None | EXP Elastomeric | Y | N | Y | 4 | 4 |
| 1040802 | 6925 | 95 | EXP Elastomeric | FIX Elastomeric | Y | N | Y | 4 | 4 |
| 1040802 | 6925 | 95 | None | EXP Elastomeric | Y | N | Y | 4 | 4 |
| 1041160 | 3980 | 115 | EXP Pot Bearing | FIX Pot Bearing | Y | N | Y | 2 | 4 |
| 1041160 | 3980 | 115 | None | EXP Pot Bearing | Y | N | Y | 2 | 4 |
| 1044839 | 65775 | 175 | FIX Elastomeric | EXP Elastomeric | Y | N | Y | 2 | 3 |
| 1045240 | 22590 | 85 | EXP Elastomeric | None | Y | N | Y | 5 | 3 |
| 1045240 | 22590 | 85 | EXP Elastomeric | FIX Elastomeric | Y | N | Y | 5 | 3 |
| 1046960 | 9224 | 81 | FIX Elastomeric | EXP Elastomeric | Y | N | Y | 2 | 2 |
| 1047010 | 21703 | 97 | FIX Elastomeric | EXP Elastomeric | Y | N | Y | 2 | 2 |
| 1052920 | 25521 | 160 | EXP Pot Bearing | FIX Pot Bearing | Y | Y | Y | 4 | 2 |
| 1052920 | 25521 | 200 | None | EXP Pot Bearing | Y | Y | Y | 4 | 2 |
| 1074590 | 7171 | 105 | EXP Elastomeric | FIX Elastomeric | N | N | N | 0 | 2 |
| 1074600 | 5400 | 70 | EXP Elastomeric | FIX Elastomeric | Y | N | Y | 2 | 2 |
| 1074600 | 5400 | 83 | FIX Elastomeric | EXP Elastomeric | Y | N | Y | 2 | 2 |
| 1074750 | 43232 | 96 | FIX Elastomeric | EXP Elastomeric | Y | N | Y | 1 | 1 |
| 1077090 | 12417 | 182 | EXP Pot Bearing | FIX Pot Bearing | Y | N | Y | 2 | 1 |

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|---------|-------|-----|-----------------|-----------------|---|---|---|---|---|
| 1077100 | 12417 | 245 | EXP Pot Bearing | FIX Pot Bearing | Y | N | Y | 3 | 1 |
| 1077100 | 12417 | 216 | FIX Pot Bearing | EXP Pot Bearing | Y | N | Y | 3 | 1 |
| 1091321 | 6925 | 92 | FIX Elastomeric | EXP Elastomeric | Y | N | Y | 3 | 4 |
| 1091322 | 6925 | 92 | FIX Elastomeric | EXP Elastomeric | Y | N | Y | 4 | 4 |
| 2262530 | 800 | 85 | EXP Elastomeric | FIX Pot Bearing | Y | N | Y | 4 | 2 |
| 2262530 | 800 | 121 | None | EXP Elastomeric | Y | N | Y | 4 | 2 |
| 2262530 | 800 | 75 | None | EXP Pot Bearing | Y | N | Y | 4 | 2 |
| 2265310 | 6005 | 115 | EXP Elastomeric | FIX Elastomeric | N | N | N | 0 | 4 |
| 3343620 | 3268 | 125 | EXP Elastomeric | FIX Elastomeric | Y | N | Y | 2 | 2 |
| 3346370 | 700 | 101 | EXP Elastomeric | FIX Elastomeric | N | N | N | 0 | 1 |
| 3346370 | 700 | 102 | None | EXP Elastomeric | N | N | N | 0 | 1 |
| 3368130 | 5600 | 175 | FIX Elastomeric | EXP Elastomeric | Y | N | Y | 1 | 2 |
| 5502121 | 21777 | 97 | FIX Elastomeric | EXP Elastomeric | Y | N | Y | 1 | 1 |
| 5502301 | 7850 | 128 | FIX Elastomeric | EXP Elastomeric | N | N | N | 0 | 1 |
| 5514160 | 2500 | 88 | EXP Pot Bearing | FIX Pot Bearing | Y | N | Y | 2 | 2 |
| 5514160 | 2500 | 117 | None | EXP Pot Bearing | Y | N | Y | 2 | 2 |
| 5523850 | 37597 | 150 | EXP Pot Bearing | FIX Pot Bearing | N | N | N | 0 | 1 |
| 1003970 | 3555 | 147 | EXP Pot Bearing | FIX Pot Bearing | N | N | N | 0 | 1 |
| 1004080 | 6923 | 184 | EXP Pot Bearing | FIX Pot Bearing | N | N | N | 0 | 1 |
| 1004370 | 1642 | 161 | EXP Elastomeric | FIX Elastomeric | N | N | N | 0 | 1 |
| 1013730 | 11650 | 96 | EXP Elastomeric | FIX Elastomeric | Y | N | Y | 3 | 1 |
| 1013730 | 11650 | 113 | None | EXP Elastomeric | Y | N | Y | 3 | 1 |
| 1017470 | 4933 | 127 | FIX Elastomeric | EXP Elastomeric | Y | N | Y | 1 | 1 |
| 1017630 | 3226 | 107 | EXP Elastomeric | FIX Elastomeric | N | N | N | 0 | 1 |
| 1017630 | 3226 | 130 | None | EXP Elastomeric | N | N | N | 0 | 1 |
| 1017640 | 3226 | 125 | EXP Elastomeric | FIX Elastomeric | Y | N | Y | 1 | 1 |
| 1017640 | 3226 | 180 | None | EXP Elastomeric | Y | N | Y | 1 | 1 |
| 1018510 | 5625 | 125 | EXP Pot Bearing | FIX Pot Bearing | N | N | N | 0 | 1 |
| 1018560 | 2705 | 87 | FIX Pot Bearing | EXP Pot Bearing | N | N | N | 0 | 2 |
| 1019900 | 2093 | 85 | EXP Elastomeric | FIX Elastomeric | N | N | N | 0 | 1 |
| 1020930 | 1614 | 100 | EXP Elastomeric | FIX Elastomeric | N | N | N | 0 | 1 |
| 1021360 | 3828 | 180 | EXP Elastomeric | FIX Elastomeric | N | N | N | 0 | 1 |
| 1024830 | 1017 | 136 | EXP Elastomeric | FIX Elastomeric | Y | N | Y | 1 | 1 |
| 1026390 | 1511 | 110 | None | FIX Elastomeric | N | N | N | 0 | 1 |
| 1026390 | 1511 | 110 | None | None | N | N | N | 0 | 1 |
| 1026440 | 757 | 75 | EXP Elastomeric | FIX Elastomeric | N | N | N | 0 | 1 |
| 1026440 | 757 | 95 | None | EXP Elastomeric | N | N | N | 0 | 1 |
| 1026440 | 757 | 75 | None | EXP Elastomeric | N | N | N | 0 | 1 |
| 1030420 | 1800 | 105 | FIX Elastomeric | EXP Elastomeric | N | N | N | 0 | 1 |
| 1030710 | 671 | 93 | None | None | N | N | N | 0 | 1 |
| 1030720 | 1671 | 123 | FIX Elastomeric | EXP Elastomeric | N | N | N | 0 | 1 |
| 1030810 | 2770 | 103 | EXP Elastomeric | FIX Elastomeric | N | N | N | 0 | 1 |
| 1030810 | 2770 | 103 | None | EXP Elastomeric | N | N | N | 0 | 1 |
| 1030850 | 1981 | 122 | EXP Elastomeric | FIX Elastomeric | N | N | N | 0 | 1 |
| 1040350 | 2628 | 90 | None | None | N | N | N | 0 | 1 |
| 1040370 | 2935 | 174 | FIX Pot Bearing | EXP Pot Bearing | N | N | N | 0 | 1 |
| 1041690 | 402 | 105 | None | None | Y | Y | N | 1 | 1 |
| 1041700 | 402 | 106 | EXP Elastomeric | FIX Elastomeric | N | N | N | 0 | 1 |
| 1041710 | 402 | 102 | FIX Elastomeric | EXP Elastomeric | N | N | N | 0 | 1 |
| 1041730 | 542 | 118 | FIX Elastomeric | EXP Elastomeric | N | N | N | 0 | 1 |
| 1045670 | 5845 | 155 | FIX Pot Bearing | EXP Pot Bearing | N | N | N | 0 | 1 |
| 1046820 | 6939 | 113 | None | None | N | N | N | 0 | 1 |
| 1050220 | 1363 | 120 | EXP Pot Bearing | FIX Pot Bearing | N | N | N | 0 | 1 |
| 1054811 | 2448 | 107 | EXP Elastomeric | FIX Elastomeric | Y | N | Y | 1 | 1 |

| | | | | | | | | | |
|---------|-------|-----|------------------|------------------|---|---|---|---|---|
| 1054811 | 2448 | 104 | None | EXP Elastomeric | Y | N | Y | 1 | 1 |
| 1054812 | 2448 | 107 | EXP Elastomeric | FIX Elastomeric | Y | N | Y | 1 | 1 |
| 1054812 | 2448 | 104 | None | EXP Elastomeric | Y | N | Y | 1 | 1 |
| 1077160 | 11972 | 86 | FIX Elastomeric | EXP Elastomeric | N | N | N | 0 | 1 |
| 1091690 | 92 | 180 | EXP Pot Bearing | FIX Pot Bearing | N | N | N | 0 | 1 |
| 1091690 | 92 | 145 | None | EXP Pot Bearing | N | N | N | 0 | 1 |
| 1091690 | 92 | 96 | None | EXP Pot Bearing | N | N | N | 0 | 1 |
| 2226190 | 13405 | 83 | EXP Pot Bearing | FIX Pot Bearing | Y | N | Y | 2 | 1 |
| 2226190 | 13405 | 134 | None | EXP Pot Bearing | Y | N | Y | 2 | 1 |
| 2226190 | 13405 | 88 | None | EXP Pot Bearing | Y | N | Y | 2 | 1 |
| 3352030 | 148 | 127 | EXP Elastomeric | FIX Elastomeric | Y | N | Y | 1 | 1 |
| 3352030 | 148 | 127 | None | EXP Elastomeric | Y | N | Y | 1 | 1 |
| 3355450 | 1242 | 125 | FIX Disc Bearing | EXP Disc Bearing | N | N | N | 0 | 1 |
| 3356240 | 2370 | 92 | FIX Elastomeric | EXP Elastomeric | Y | N | Y | 1 | 1 |

Note 1: BIN = Bridge Identification Number

APPENDIX B
STATISTICAL ANALYSIS

STATISTICAL ANALYSIS

One-way Analysis of Variance (ANOVA) was performed to assist in determining the correlation between each of the variables (bridge vibration, traffic volume, span length, and bearing type) and deck cracking. The F-test was used to determine if there are any significant differences amongst the means. If there are, the multiple range tests were used to determine which means are significantly different from others. Multi-factor ANOVA was used to examine the effects of two or more factors (i.e. interaction effects) on deck cracking. Data from all 383 bridge spans was used in the analysis. If inspectors rated the bridge vibration or crack ratings with a non-integer, the ratings were rounded to the nearest integer (eg.1.5 was treated as 2 for the analysis).

Effect of Vibration

ANOVA was performed to determine the correlation between vibration severity and observed deck cracking severity (SEV). The results are shown in Tables B1 and B2. Modified vibration ratings (CVIB) shown in Fig. 6 in Section IV along with deck cracking ratings shown in Fig. 4 were used in this analysis.

Table B1. ANOVA table for cracking severity (SEV) by modified vibration ratings (CVIB).

| Source | Sum of Squares | Degrees of Freedom | Mean Square | F-Ratio | P-Value |
|----------------|----------------|--------------------|-------------|---------|---------|
| Between groups | 228.262 | 2 | 114.131 | 92.92 | 0.0000 |
| Within groups | 466.751 | 380 | 1.22829 | | |
| Total (Corr.) | 695.013 | 382 | | | |

Table B2. Table of means for cracking severity (SEV) by modified vibration ratings (CVIB) with 95% confidence intervals.

| CVIB | COUNT | Mean | Std. Err. (Pooled s) | Lower Limit | Upper Limit |
|--------------|-------|----------|-------------------------|-------------|-------------|
| 1 (Low) | 217 | 0.617512 | 0.0752351 | 0.512909 | 0.722114 |
| 3 (Moderate) | 143 | 1.78322 | 0.0926793 | 1.65436 | 1.91207 |
| 5 (High) | 23 | 3.34783 | 0.231093 | 3.02653 | 3.66912 |
| Total | 383 | 1.21671 | | | |

Note that the ANOVA table decomposes the variance of SEV into two components: a between-group component and a within-group component. The F-ratio, which in this case equals 92.9187, is a ratio of the between-group estimate to the within-group estimate. Since the P-value of the F-test is less than 0.05, there is a statistically significant difference between the mean SEV from one level of CVIB to another at the 95.0% confidence level. To determine which means are significantly different from which others, multiple range tests were used.

Table B3. Multiple range tests for cracking severity (SEV) by modified vibration ratings (CVIB).

| CVIB | Count | Mean | Homogeneous Groups |
|----------|-------|------------|--------------------|
| 1 | 217 | 0.617512 | X |
| 3 | 143 | 1.78322 | X |
| 5 | 23 | 3.34783 | X |
| Contrast | | Difference | +/- Limits |
| 1 - 3 | | *-1.16571 | 0.234714 |
| 1 - 5 | | *-2.73031 | 0.477856 |
| 3 - 5 | | *-1.56461 | 0.489561 |

* denotes a statistically significant difference.

Table B3 applies a multiple comparison procedure to determine which means are significantly different from others. The bottom half of the table shows the estimated difference between each pair of means. The asterisks placed next to 3 pairs, indicate that these pairs show statistically significant differences at the 95% confidence level. Three homogenous groups are identified using columns of X's. Within each column, the levels containing X's form a group of means that have no statistically significant differences. Fisher's least significant difference (LSD) procedure was used to discriminate among the means. With this method, there is a 5% risk of calling each pair of means significantly different when the actual difference equals 0.

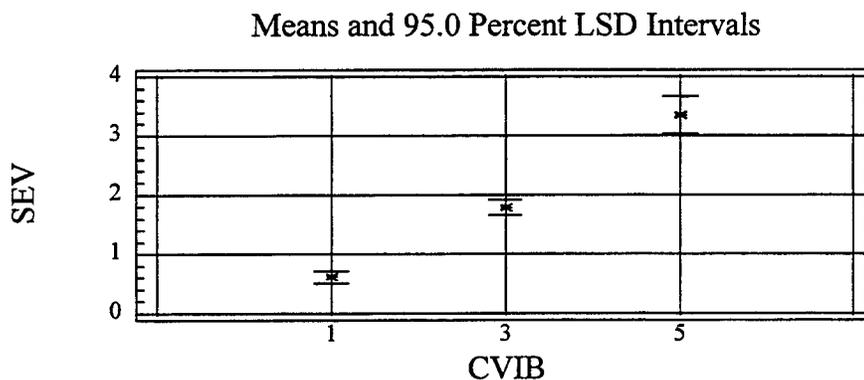


Figure B1. Means plot for cracking severity (SEV) and modified vibration ratings (CVIB).

The means plot (Fig. B1) shows the mean SEV for each level of CVIB. It also shows an interval around each mean. The intervals are based on Fisher's least significant difference (LSD) procedure. They are constructed in such a way that if two means are the same, their intervals will overlap 95%

of the time. Any pair of intervals that do not overlap vertically correspond to a pair of means which have a statistically significant difference. This indicates that there are three significantly different means.

From all the above data, it can be concluded that the vibration severity significantly influences the cracking severity. Similar analysis was performed for other parameters.

Effect of Traffic Volume

For analysis, the traffic volume data, i.e. Average Annual Daily Traffic (AADT), was classified into three groups: low volume ($AADT \leq 1000$), medium volume ($1000 < AADT \leq 5000$), and high volume ($AADT > 5000$). The groups were designated 1, 2, and 3 respectively. Analyses similar to those described earlier were conducted and results are given in Tables B4-B6 and Fig. B2.

Table B4. ANOVA table for cracking severity (SEV) by traffic volume (AADT).

| Source | Sum of Squares | Degrees of Freedom | Mean Square | F-Ratio | P-Value |
|----------------|----------------|--------------------|-------------|---------|---------|
| Between groups | 36.6719 | 2 | 17.3359 | 9.98 | 0.0001 |
| Within groups | 660.341 | 380 | 1.73774 | | |
| Total (Corr.) | 695.013 | 382 | | | |

Since the P-value of the F-test is less than 0.05, there is a statistically significant difference between the mean SEV from one level of AADT to another at the 95% confidence level. Thus, means plot and multiple range tests were conducted for further analysis.

Table B5. Table of means for cracking severity (SEV) by traffic volume (AADT) with 95% confidence intervals.

| AADT | COUNT | Mean | Std. Err. (Pooled s) | Lower Limit | Upper Limit |
|-------|-------|----------|----------------------|-------------|-------------|
| 1 | 89 | 0.674157 | 0.139732 | 0.479882 | 0.868432 |
| 2 | 124 | 1.33065 | 0.118381 | 1.16606 | 1.49523 |
| 3 | 170 | 1.41765 | 0.101104 | 1.27708 | 1.55822 |
| Total | 383 | 1.21671 | | | |

Table B6. Multiple range tests for cracking severity (SEV) by traffic volume (AADT).

| AADT | Count | Mean | Homogeneous Groups |
|------|-------|----------|--------------------|
| 1 | 89 | 0.674157 | X |
| 2 | 124 | 1.33065 | X |
| 3 | 170 | 1.41765 | X |

| Contrast | Difference | +/- Limits |
|----------|------------|------------|
| 1 - 2 | *-0.656488 | 0.36009 |
| 1 - 3 | *-0.74349 | 0.339123 |
| 2 - 3 | -0.0870019 | 0.306101 |

* denotes a statistically significant difference

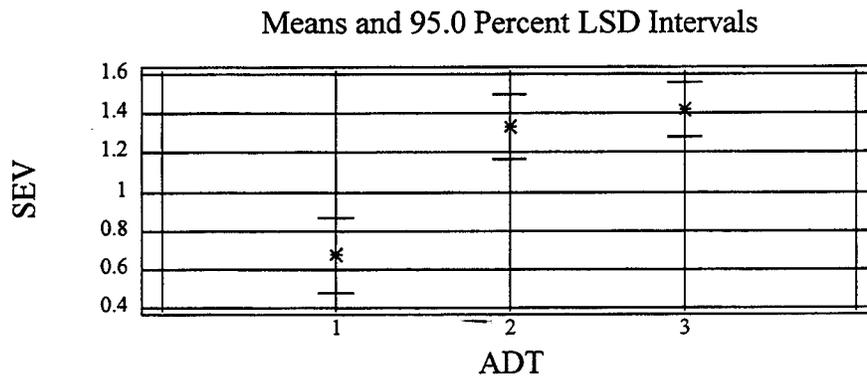


Figure B2. Means plot for traffic volume (AADT) and cracking severity (SEV).

The results shown in Tables B5 and B6, and Fig. B2 indicate that there is no statistically significant differences between cracking of medium and high volume bridges, indicating that they can be combined for further analysis. At the same time, it also indicates that AADT does influence the cracking severity and very low volume bridges exhibit less cracking. This confirms what is expected from practice. Thus, for a multi-factor ANOVA, only two groups will be used, low volume (AADT \leq 1000) and high volume (AADT > 1000).

Effect of Span Length

For analysis, the bridges were classified based on span length into three groups: small spans 30-m or shorter (LEN = 3), medium spans between 30 m and 60 m long (LEN = 2), and long spans which are greater than 60 m (LEN = 1). Analysis results are shown in Tables B7-B9, and Fig. B3. Since the P-value of the F-test is less than 0.05, there is a statistically significant difference between the mean SEV from one level of span length (LEN) to the another at the 95% confidence level. Thus, means plot and multiple range tests were conducted for further analysis.

Table B7. ANOVA table for cracking severity (SEV) by span lengths (LEN).

| Source | Sum of Squares | Degrees of Freedom | Mean Square | F-Ratio | P-Value |
|----------------|----------------|--------------------|-------------|---------|---------|
| Between groups | 17.9466 | 2 | 8.97331 | 5.04 | 0.0069 |
| Within groups | 677.066 | 380 | 1.78175 | | |
| Total (Corr.) | 695.013 | 382 | | | |

Table B8. Table of means for cracking severity (SEV) by span lengths (LEN) with 95% confidence intervals.

| AADT | COUNT | Mean | Std. Err. (Pooled s) | Lower Limit | Upper Limit |
|-------|-------|---------|----------------------|-------------|-------------|
| 1 | 22 | 2.09091 | 0.284585 | 1.69524 | 2.48658 |
| 2 | 258 | 1.17442 | 0.0831025 | 1.05888 | 1.28996 |
| 3 | 103 | 1.13592 | 0.131524 | 0.95306 | 1.31878 |
| Total | 383 | 1.21671 | | | |

Table 9. Multiple range tests for cracking severity (SEV) by span length.

| Len | Count | Mean | Homogeneous Groups |
|-----|-------|---------|--------------------|
| 3 | 103 | 1.13592 | X |
| 2 | 258 | 1.17442 | X |
| 1 | 22 | 2.09091 | X |

| Contrast | Difference | +/- Limits |
|----------|------------|------------|
| 1 - 2 | *0.91649 | 0.582929 |
| 1 - 3 | *0.954987 | 0.616429 |
| 2 - 3 | 0.0384963 | 0.305903 |

*denotes a statistically significant difference

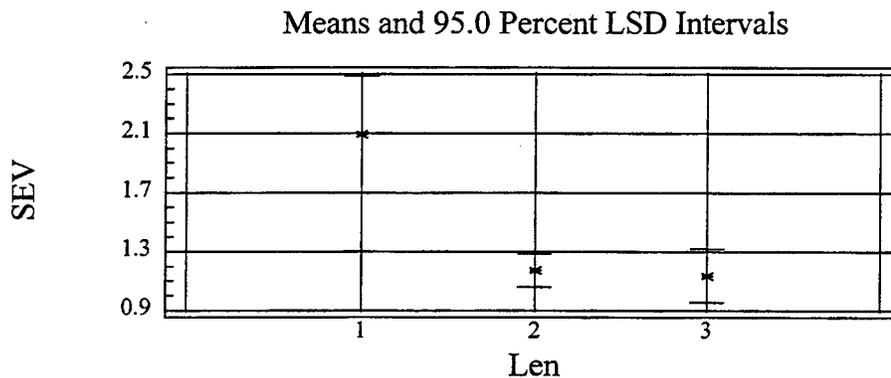


Figure B3. Means plot for span lengths (LEN) and cracking severity (SEV).

The results from Tables B8 and B9, and Fig. B3 indicate that there is no statistically significant differences between cracking of bridges with spans less than 30 m long, and spans between 30 m to 60 m long, indicating that they can be combined. At the same time, it also indicates that span length does influence the cracking severity, with longer spans exhibiting more cracking. Thus, for a multi-factor ANOVA, only two groups will be used, spans 60 m or shorter, and spans longer than 60 m.

Effect of Bearings

Influence of bearings on deck cracking severity was examined. Since there are many different types of bearings, they were classified into 6 groups, as following.

1. Elastomeric Bearing (Free/Expansion)
2. Elastomeric Bearing (Fixed)
3. Pot Bearing (Fixed)
4. Pot Bearing (Free/Expansion)
5. None
6. Others (include discs, rockers, multi-rotational, etc.)

Analysis results are given in Tables B10-B11, and Figs. B4-B5, for beginning (BEGBEAR) and end bearings (ENDBEAR). The results indicate that there is no statistically significant difference between the cracking severity and type of bearing. Thus, type of bearing is not considered in further analysis.

Table B10. ANOVA table for beginning bearing type (BEGBEAR) by cracking severity (SEV).

| Source | Sum of Squares | Degrees of Freedom | Mean Square | F-Ratio | P-Value |
|----------------|----------------|--------------------|-------------|---------|---------|
| Between groups | 16.527 | 2 | 3.30539 | 1.84 | 0.1048 |
| Within groups | 678.486 | 380 | 1.7997 | | |
| Total (Corr.) | 695.013 | 382 | | | |

Table B11. ANOVA table for end bearing type (ENDBEAR) by cracking severity (SEV).

| Source | Sum of Squares | Degrees of Freedom | Mean Square | F-Ratio | P-Value |
|----------------|----------------|--------------------|-------------|---------|---------|
| Between groups | 7.4899 | 2 | 1.49798 | 0.82 | 0.5350 |
| Within groups | 687.523 | 380 | 1.82367 | | |
| Total (Corr.) | 695.013 | 382 | | | |

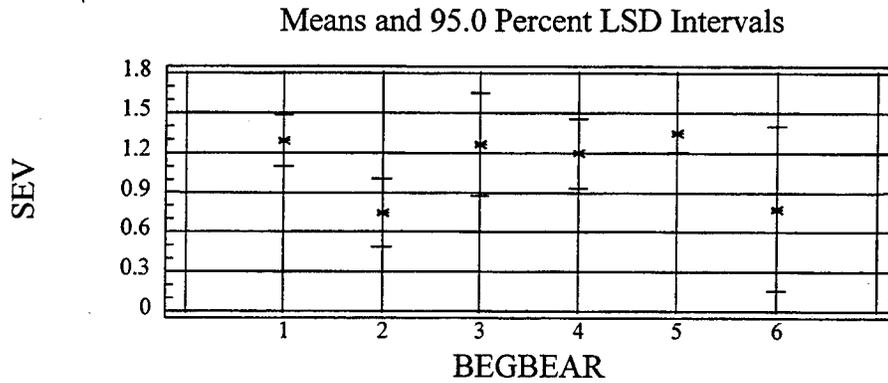


Figure B4. Means plot for beginning bearing type (BEGBEAR) and cracking severity (SEV).

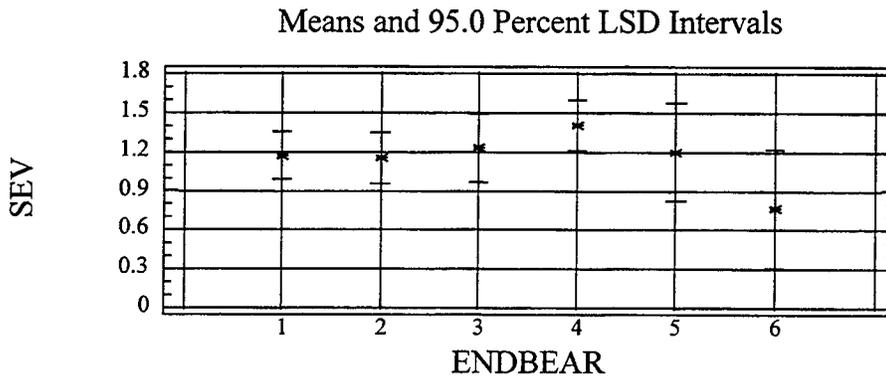


Figure B5. Means plot for end bearing type (ENDBEAR) and cracking severity (SEV).

Multi-factor Analysis of Variance

Multi-factor ANOVA is useful in examining the effects of two or more factors on one variable. Thus, multi-factor ANOVA is used here to examine the effect of bridge vibration, span length, and traffic volume (AADT) on bridge deck cracking. As illustrated in the previous section, bridge vibration is divided into 3 ranges - low (1), medium (3), and noticeable or severe (5). The traffic volume was divided into two categories - low with $AADT \leq 1000$ (1), and high with $AADT > 1000$ (3). Similarly, span lengths have been divided into two categories - short spans of length ≤ 60 m (3), and large spans, which are longer than 60 m (1).

This analysis is to determine the factors having a statistically significant effect on deck cracking severity (SEV), and also test for significant interactions amongst the factors. The F-tests in the ANOVA table identify the significant factors. For each significant factor, multiple range tests tell which means are significantly different from others.

Table B12 decomposes the severity of deck cracking (SEV) into contributions by various factors. The contribution of each factor is measured by having the effects of all other factors removed. The P-values test the statistical significance of each factor. Since P-values of vibration severity and span length are less than 0.05, these have a statistically significant effect on bridge deck cracking at the 95% confidence level.

Table B12. ANOVA table for deck cracking severity (SEV).

| Source | Sum of Squares | Degrees of Freedom | Mean Square | F-Ratio | P-Value |
|----------------------|----------------|--------------------|-------------|---------|---------|
| A: CVIB | 42.9662 | 2 | 21.4831 | 20.38 | 0.0000 |
| B: AADT | 0.30207 | 1 | 0.30207 | 0.290 | 0.5928 |
| C: LEN | 18.0213 | 1 | 18.0213 | 17.09 | 0.0000 |
| Interactions | | | | | |
| AB | 2.35954 | 2 | 1.17977 | 1.120 | 0.3277 |
| AC | 49.9581 | 2 | 24.9717 | 23.69 | 0.0000 |
| BC | 2.38117 | 1 | 2.38117 | 2.260 | 0.1337 |
| RESIDUAL | 393.262 | 373 | 1.05432 | | |
| TOTAL (Corrected) | 695.013 | 382 | | | |

Note: All F-ratios are based on the residual mean square error.

Figs B6-B8 show the mean deck cracking (SEV) for each level of vibration severity (CVIB), traffic volume (AADT), and span lengths (LEN), along with 95% confidence intervals for each of the means. The bars which do not overlap indicate significant difference between the two means, and bars that overlap indicate no significant difference between the means. The interaction plots are useful for interpreting the interaction between vibration severity, traffic volume, and span length. For example, the two lines drawn on Fig. B9 represent each level of span length. They connect the least squares means for the 3 levels of vibration severity (CVIB). If there was absolutely no interaction, these lines would be parallel. Stronger the interaction, larger the difference in shape of these lines. This plot and the p value of lower than 0.05 for interaction effect (AC) in the means table indicate that interaction exists between vibration severity and span lengths.

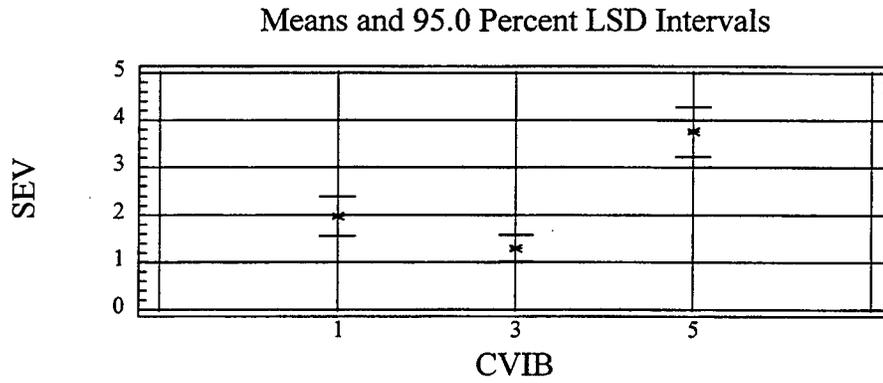


Figure B6. Means plot for deck cracking severity (SEV) and vibration severity (CVIB).

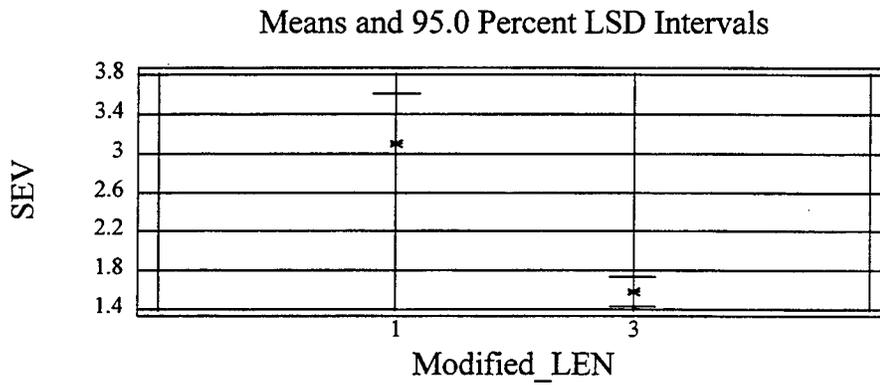


Figure B7. Means plot for deck cracking severity (SEV) and span length (LEN).

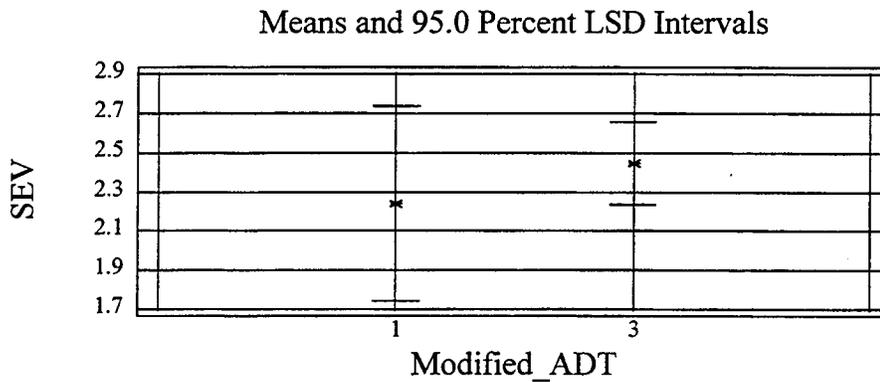


Figure B8. Means plot for deck cracking severity (SEV) and traffic volume (AADT).

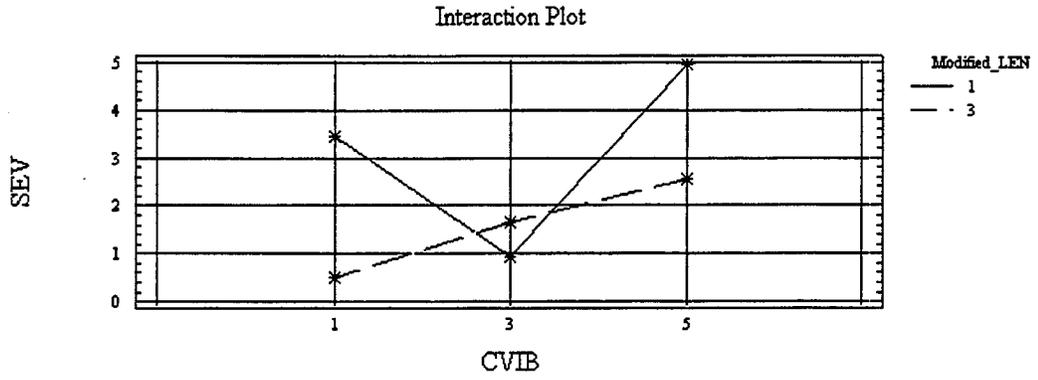


Figure B9. Interaction plot for deck cracking severity (SEV), vibration severity (CVIB), and span length (LEN).